

## PRECALCULUS ACCELERATED

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Spring Final Exam Practice

**PART 1: CALCULATOR REQUIRED**

Name: \_\_\_\_\_

Date: \_\_\_\_\_ Period: \_\_\_\_\_

**Directions:** Complete each of the following NEATLY IN PENCIL in the space provided. Show all work. Round at **THREE** decimal places. Good luck!

**Multiple Choice:**

1. 
$$\lim_{x \rightarrow 0} \frac{\sqrt{49 - x^2} - 7}{9x} =$$

(a)  $-\frac{1}{9}$

(b)  $-\frac{7}{9}$

(c) 1

(d) 0

(e) DNE

2. The graph of  $f(x) = \ln(x^2 - 9)$  has a critical value at

(a) 3

(b) 9

(c)  $\pm 3$

(d) 0

(e) The graph has no critical values

3. If  $\log_4 x + 3\log_4 x = 9$ , then  $x =$ 

(a) 1.86

(b) 2.25

(c) 9

(d) 22.6

(e) 256

6. If  $y = \frac{-1}{3x^2 - 2}$ , then  $\frac{dy}{dx} =$

(a)  $\frac{-3x^2 + 6x + 2}{(3x^2 - 2)^2}$

(b)  $\frac{-3x^2 + 6x + 2}{3x^2 - 2}$

(c)  $\frac{6x}{(3x^2 - 2)^2}$

(d)  $\frac{6x}{3x^2 - 2}$

(e)  $-\frac{1}{6x}$

**Free Response:**

1. Find the domain, vertical asymptotes, zeroes, and extreme points of  $y = \ln(2x^2 - 9x + 6)$ .

Domain:

Vertical Asymptotes:

Extreme points:

Zeroes:

A.M.D.G.

2. Find the domain and extreme points of  $y = e^{x^3-3x^2}$ .

Domain:

Extreme points:

3. Find the domain, vertical asymptotes, zeroes, POEs, and extreme points of  $f(x) = \frac{x^3 - 16x}{x^3 - x^2 - 20x}$ .

Domain:

Vertical Asymptotes:

POEs:

Zeroes:

Extreme points:

A.M.D.G.

4. Find the zeros and extreme points of  $y = 2x^3 + 9x^2 - 33x + 14$ .

Zeros:

Extreme points:

**Directions:** Complete each of the following NEATLY IN PENCIL in the space provided. Show all work. Round at **THREE** decimal places. Good luck!

**Multiple Choice:**

7. If  $f(x) = \frac{x-6}{1-x}$ , what is the value of  $f'(2)$  ?

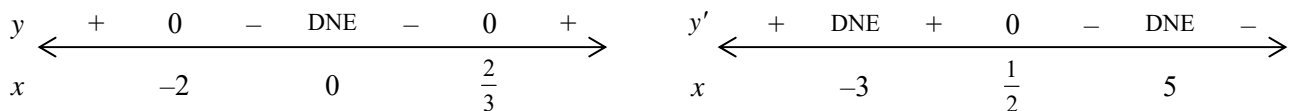
- (a) DNE
- (b) -5
- (c) -4
- (d) 1
- (e) -1

8. Which of the following is true about the function  $f$  if  $f(x) = \frac{x^2 + x - 2}{2x^2 + x - 3}$  ?

- I.  $f$  has a zero at  $x = 1$ .
- II. The graph of  $f$  has a POE at  $x = 1$ .
- III. The graph of  $f$  has a horizontal asymptote at  $y = \frac{1}{2}$ .

- (a) II only    (b) I and II only    (c) I and III only    (d) II and III only    (e) I, II and III

9. Given these sign patterns, which of the following statements is/are true?



- I. There is a zero at  $x = \frac{1}{2}$
- II. The function is increasing on  $x \in (-\infty, -2) \cup \left(\frac{2}{3}, \infty\right)$
- III. There is a maximum at  $x = -2$

- (a) I and III    (b) II only    (c) II and III    (d) I, II, and III    (e) None of these

$$10. \lim_{x \rightarrow -\infty} \frac{10^8 x^5 + 10^6 x^4 + 10^4 x^2}{10^9 x^6 + 10^7 x^5 + 10^5 x^3}$$

- (a) 0      (b) 1      (c) -1      (d)  $\frac{1}{10}$       (e)  $-\frac{1}{10}$

**Free Response:**

5. Find all traits and sketch  $y = 2x^3 + 9x^2 - 33x + 14$ . **SIGN PATTERN OF THE DERIVATIVE REQUIRED FOR FULL CREDIT!**

Domain:

Zeros:

y-intercept:

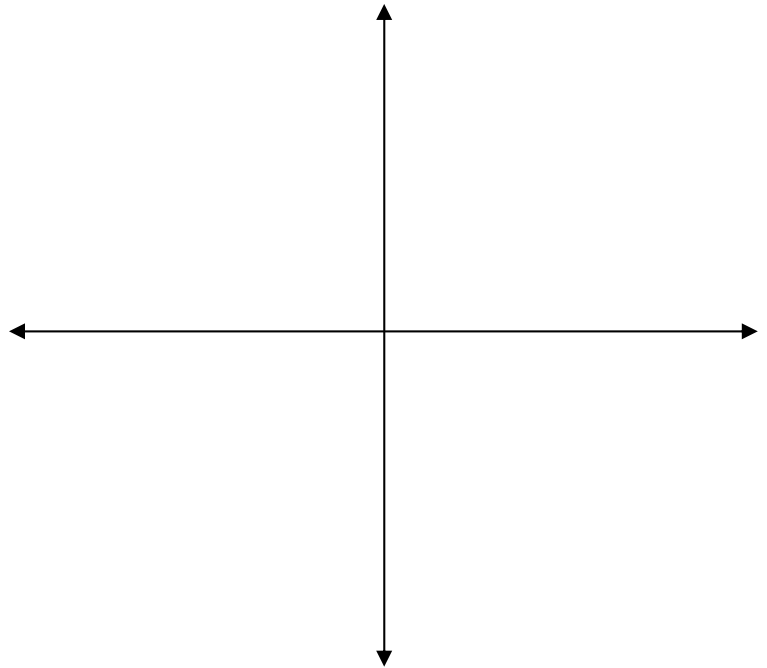
VAs:

EB:

POEs:

Extreme points:

Range:



A.M.D.G.

6. Find all traits and sketch  $f(x) = \frac{x^3 - 16x}{x^3 - x^2 - 20x}$ . **SIGN PATTERN OF THE DERIVATIVE REQUIRED FOR FULL CREDIT!**

Domain:

Zeros:

y-intercept:

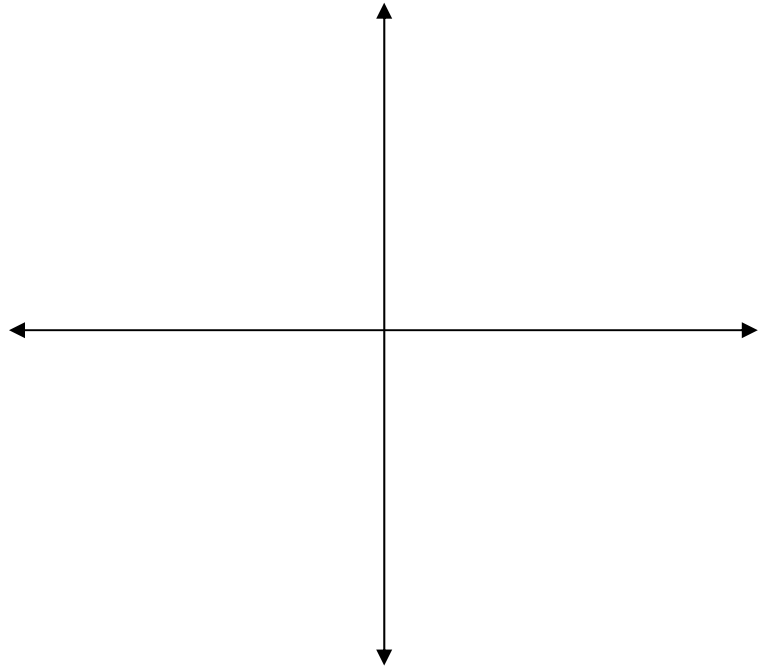
VAs:

EB:

POEs:

Extreme points:

Range:



A.M.D.G.

7. Find all traits and sketch  $f(x) = \ln(16 + 6x - x^2)$ . **SIGN PATTERN OF THE DERIVATIVE REQUIRED FOR FULL CREDIT!**

Domain:

Zeros:

y-intercept:

VAs:

EB:

POEs:

Extreme points:

Range:

