

Math Analysis Worksheet 2

4.1 Identities

Prove the following identities.

1. $\sin^2 \theta + \tan^2 \theta + \cos^2 \theta = \sec^2 \theta$

2. $\sec^2 \theta + \csc^2 \theta = \sec^2 \theta \csc^2 \theta$

3. $\cos x (\sec x - \cos x) = \sin^2 x$

$$4. \tan x + \cot x = \sec x \csc x$$

$$5. \cos x (\sec x + \cos x \csc^2 x) = \csc^2 x$$

$$6. \frac{(\cos x - \sin x)^2}{\sin x} = \csc x - 2 \cos x$$

$$7. \frac{\cos x}{\sec x} + \frac{\sin x}{\csc x} = 1$$

$$8. \frac{\cos x}{1 - \sin x} + \frac{1 - \sin x}{\cos x} = 2 \sec x$$

$$9. \frac{\cos x \sec x}{\tan x} = \cot x$$