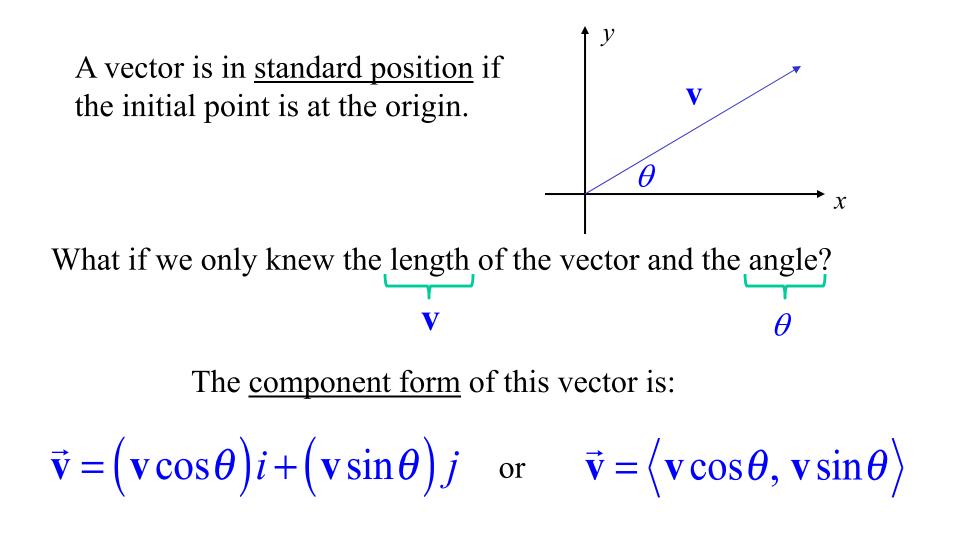
A-6 Vectors

Standard A6a: Find and draw a resultant vector from other component vectors.

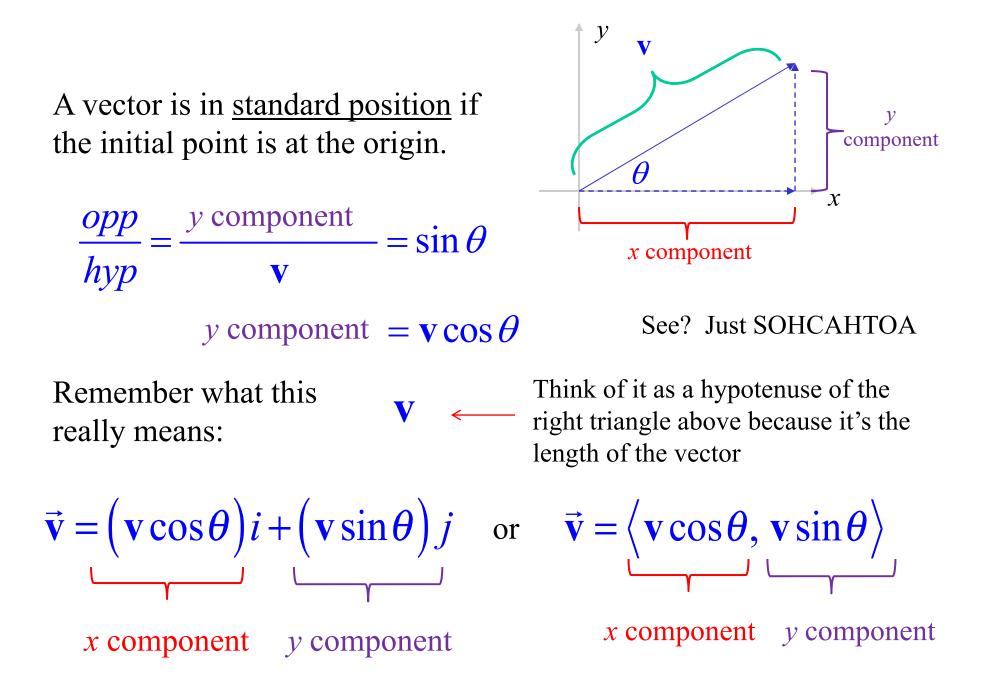
Standard A6b: Find the direction angle of a resultant vector from other component vectors.



Before anyone panics, this is just SOHCAHTOA...

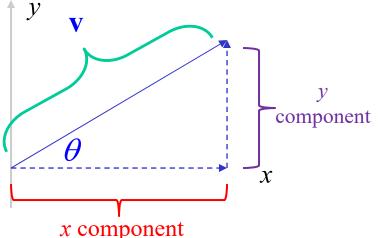
Just watch...

y V A vector is in standard position if the initial point is at the origin. X $=\frac{x \text{ component}}{\mathbf{v}} = \cos\theta$ x component hyp x component = $\mathbf{v} \cos \theta$ Think of it as a hypotenuse of the Remember what this V right triangle above because it's the really means: length of the vector $\vec{\mathbf{v}} = (\mathbf{v}\cos\theta)i + (\mathbf{v}\sin\theta)j$ or $\vec{\mathbf{v}} = \langle \mathbf{v}\cos\theta, \mathbf{v}\sin\theta \rangle$ x component x component



If it's the angle that you need to find, then you need to know this:

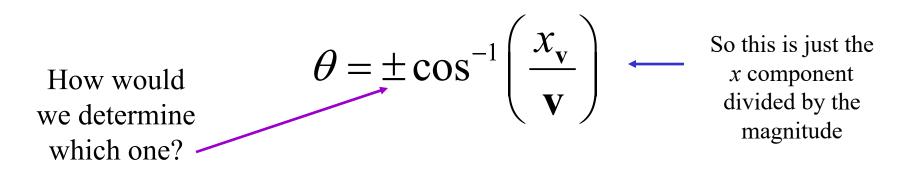
Remember that the magnitude and components form a right triangle



The direction of a vector **v** is found this way:

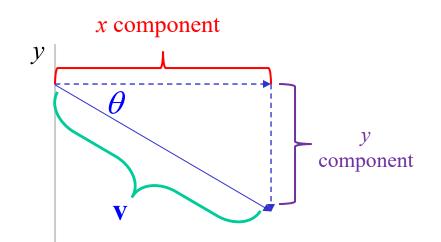
$$\cos\theta = \frac{adj}{hyp} = \frac{x \text{ component}}{\mathbf{v}} = \frac{x_{\mathbf{v}}}{\mathbf{v}}$$

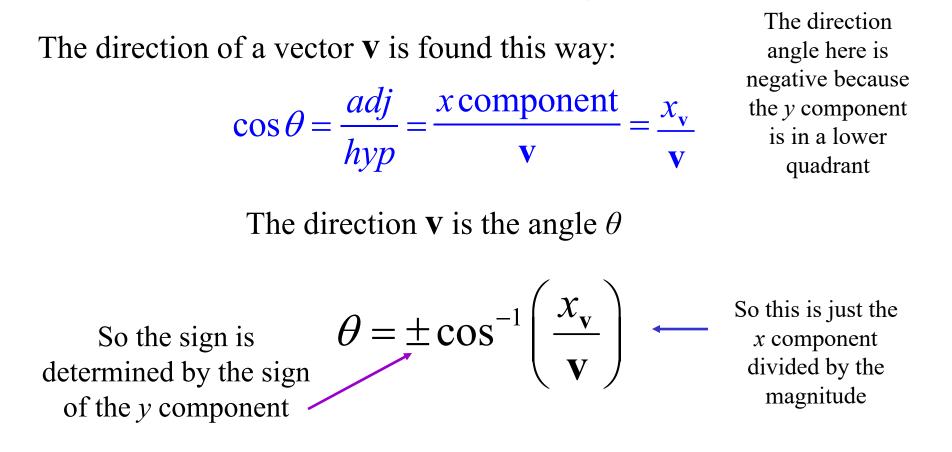
The direction **v** is the angle θ



If it's the angle that you need to find, then you need to know this:

Remember that the magnitude and components form a right triangle

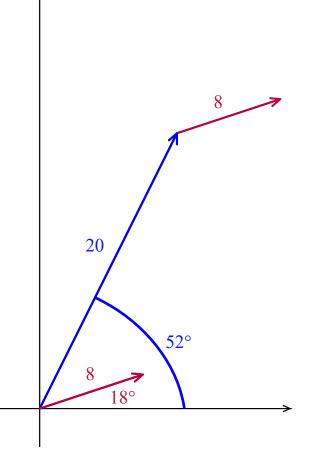




The current of the water at this time is 8 mph with a direction of 18° north of east

How does the current affect the speed and direction of the boat?

In other words find the vector that results from adding the first two vectors.



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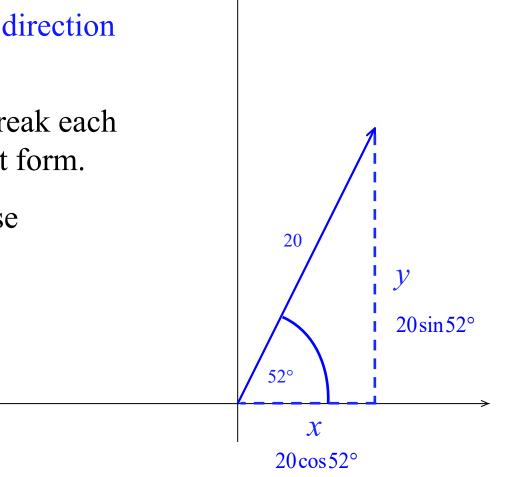
The sum of these two vectors will look like this.

In order to do add them we will have to break them into their *x* and *y* components one vector at a time.

In order to add them we need to break each down into their *x* and *y* component form.

Notice the right triangle so let's use SOHCAHTOA

 $\frac{y}{20} = \sin 52^{\circ}$ $y = 20\sin 52^{\circ}$

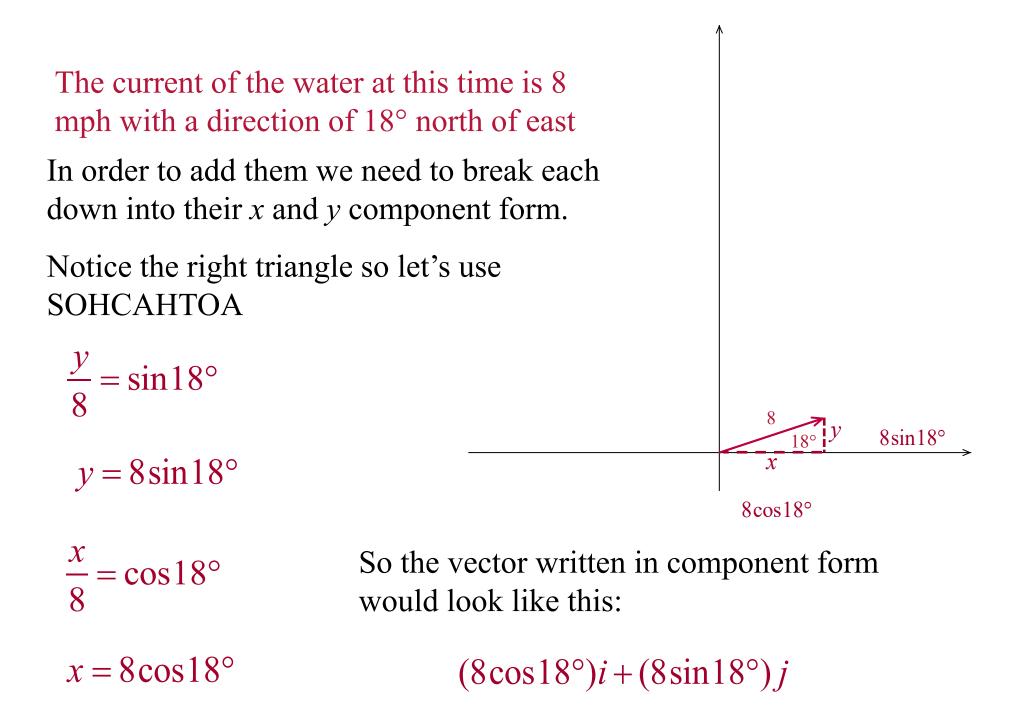


 $\frac{x}{20} = \cos 52^{\circ}$

So the vector written in component form would look like this:

 $x = 20\cos 52^\circ$

 $(20\cos 52^\circ)i + (20\sin 52^\circ)j$



The current of the water at this time is 8 mph with a direction of 18° north of east

How does the current affect the speed and direction of the boat?

In other words find the vector that results from adding the first two vectors.

Now we just add their corresponding components

 $(8\cos 18^\circ)i + (8\sin 18^\circ)j$

 $(20\cos 52^\circ)i + (20\sin 52^\circ)j$

 $(20\cos 52^\circ + 8\cos 18^\circ)i + (20\sin 52^\circ + 8\sin 18^\circ)j$

The current of the water at this time is 8 mph with a direction of 18° north of east

How does the current affect the speed and direction of the boat?

In other words find the vector that results from adding the first two vectors.

We'll use the calculator to find the actual values $(20\cos 52^\circ + 8\cos 18^\circ)i + (20\sin 52^\circ + 8\sin 18^\circ)j$

19.922*i*+18.232*j*

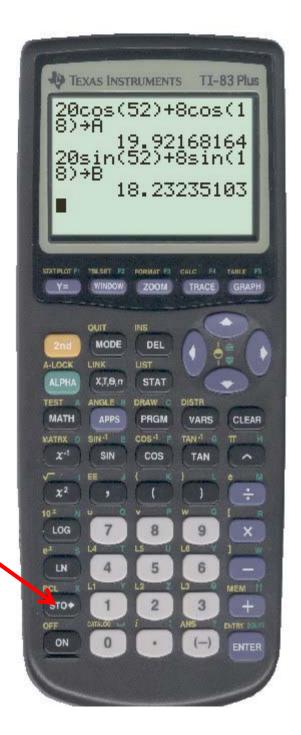
Note that we stored the values which will be explained shortly



We'll use the calculator to find the actual values we don't want to round anything until we have our final answer.

Enter your calculations then press this button followed by any letter.

The calculator stores the exact values here in A and B so we can use them later.



The current of the water at this time is 8 mph with a direction of 18° north of east

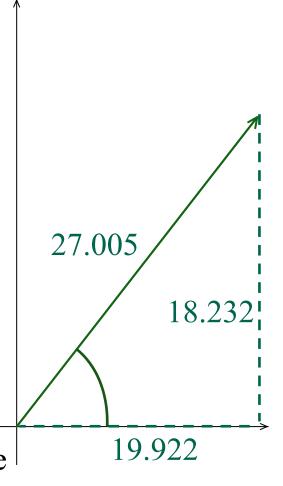
How does the current affect the speed and direction of the boat?

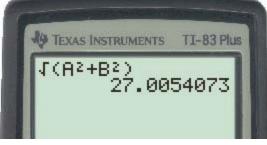
In other words find the vector that results from adding the first two vectors.

The speed is the length of this new vector which we can find using the Pythagorean Theorem and the stored values in the calculator.

27.005 mph

But what about it's new direction?





The current of the water at this time is 8 mph with a direction of 18° north of east

How does the current affect the speed and direction of the boat?

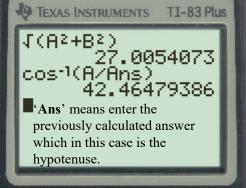
In other words find the vector that results from adding the first two vectors.

Remembering the slide about inverse cosine, we just take the x component (adjacent) and divide it by the speed we just found (hypotenuse)

42.465°

And we know it's positive because the *y* component is positive. We can also see this because it is in the first quadrant.

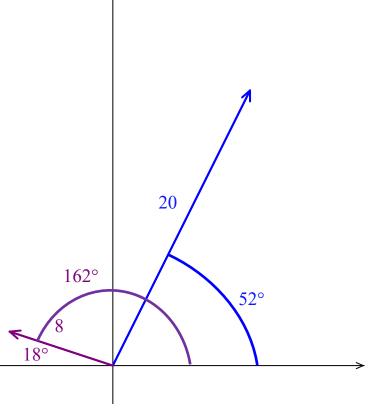
27.005 18.232 42.465° 19.922



This time the current of the water is 8 mph with a direction of 18° north of west

How does the current affect the speed and direction of the boat?

This time we will have to do a little more work with the direction angles?



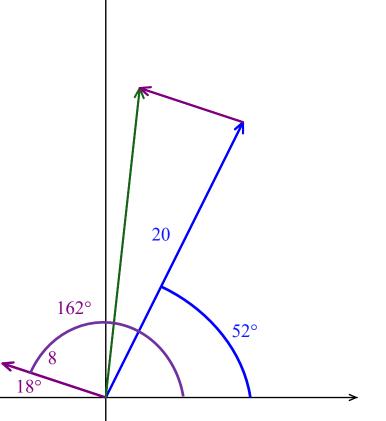
 $(20\cos 52^\circ)i + (20\sin 52^\circ)j$ $(8\cos 162^\circ)i + (8\sin 162^\circ)j$

 $(20\cos 52^\circ + 8\cos 162^\circ)i + (20\sin 52^\circ + 8\sin 162^\circ)j$

This time the current of the water is 8 mph with a direction of 18° north of west

How does the current affect the speed and direction of the boat?

This time we will have to do a little more work with the direction angles?



EXAS INSTRUMENTS

20cos(52)+8cos(1

18.23235103

TI-83 Plus

 $(20\cos 52^\circ + 8\cos 162^\circ)i + (20\sin 52^\circ + 8\sin 162^\circ)j$

4.705*i*+18.232*j*

This time the current of the water is 8 mph with a direction of 18° north of west

How does the current affect the speed and direction of the boat?

This time we will have to do a little more work with the direction angles?

4.705*i*+18.232*j*

$$\sqrt{(4.705)^2 + (18.232)^2} \approx 18.830$$
$$\cos^{-1}\left(\frac{4.705}{\sqrt{(4.705)^2 + (18.232)^2}}\right) \approx 75.531^\circ$$

