Determine if the given series converges or diverges. Indicate the method that you use and show the work that leads to your conclusion.

$$1) \sum_{n=1}^{\infty} e^{-n}$$

$$4) \sum_{n=1}^{\infty} \left(\frac{1}{n}\right)$$

2) 
$$\sum_{n=1}^{\infty} \frac{1}{e^n + 1}$$

$$5) \sum_{n=1}^{\infty} \left(\frac{2}{n}\right)^{e}$$

$$3) \sum_{n=1}^{\infty} \frac{1}{e^n - 3}$$

$$6) \sum_{n=1}^{\infty} \left( \frac{1}{n+2} \right)^{e}$$

$$7) \sum_{n=1}^{\infty} \frac{\sqrt{n^3 + 5}}{\sqrt{n^5 + 7}}$$

8) 
$$\sum_{n=1}^{\infty} \frac{n+1}{n2^n}$$

$$9) \sum_{n=1}^{\infty} \frac{2^n}{3^n}$$

For exercises 10 and 11, prove that the series converges and find its sum.

10) 
$$\sum_{n=1}^{\infty} \frac{2^n + 1}{3^n}$$

11) 
$$\sum_{n=0}^{\infty} \frac{3}{n^2 + 4n + 3}$$