

AP Statistics
Mr Murphy
Hypothesis Testing and Confidence Intervals
for proportions worksheet

Name:
Date:
Period:

A.M.D.G.

Formulae:

Confidence Intervals (generally): statistic \pm (critical value)(standard deviation)

One Proportion:

Confidence Interval

$$\hat{p} \pm z \sqrt{\frac{\hat{p}(1-\hat{p})}{n}}$$

Hypothesis Testing

$$z = \frac{\hat{p} - p}{\sqrt{\frac{p(1-p)}{n}}}$$

Two Proportions:

Confidence Interval

$$\hat{p}_1 - \hat{p}_2 \pm z \sqrt{\frac{\hat{p}_1(1-\hat{p}_1)}{n_1} + \frac{\hat{p}_2(1-\hat{p}_2)}{n_2}}$$

Hypothesis Testing

$$z = \frac{\hat{p}_1 - \hat{p}_2}{\sqrt{\hat{p}_c(1-\hat{p}_c)\left(\frac{1}{n_1} + \frac{1}{n_2}\right)}}$$

$$\hat{p}_c = \frac{x_1 + x_2}{n_1 + n_2}$$

Confidence Level (CI)	z Critical Value (C.V.)
90%	1.645
95%	1.96
99%	2.58

Type I Error: (false positive) – rejecting the null hypothesis in favor of the alternative when the null hypothesis is actually true.

Type II Error: (false negative) – failing to reject the null hypothesis (rejecting the alternative) when the alternative hypothesis is actually true.

Process for Hypothesis Testing:

1. State the null H_0 and alternate hypotheses H_a . Be sure to define parameters
2. Give the significance level α
3. Identify the inference procedure (in this case it is a single proportion z test)
4. Verify that the conditions for the procedure are met (check assumptions)
5. Calculate the test statistic z and p -value. Sketching a picture of the situation can help and is recommended.

$$z = \frac{\hat{p} - p}{\sqrt{\frac{p(1-p)}{n}}}$$

6. Make an inference based on the p -value (you do not need to interpret the p -value unless specifically asked)

For this state the inference in two sentences -

- A. Summarize in theory discussing H_0 . Always start by stating the P - value compared to the significance level, α , of the test
 - If the P - value is **less than** α , then we **reject the null hypothesis (H_0)** at the significance level we tested.
 - If the P - value is **greater than** α , then we **fail to reject the null hypothesis (H_0)** at the significance level we tested.
- B. Summarize in context discussing H_a .
 - **If we reject H_0** state that “we have evidence that the proportion of _____ is ..., therefore, the (*initial claim*) is incorrect.”
 - **If we fail to reject H_0** state that “we have insufficient evidence that the proportion of _____ is ..., therefore, we cannot reject the (*initial claim*).”

Interpreting Confidence Interval and Level:

Confidence Intervals

“We are (confidence level) % confident that p , the true proportion of (proportion in context of problem), is between ____% and ____%.”

Confidence Level

“We used a method to construct this estimate that in the long run will successfully capture the true value of p (confidence level) % of the time.”

1. Mr. Maychrowitz was recently playing through the video game “Dark Souls” again, and noticed that the drop rate of a certain item was approximately 15.7% (after creating a sampling distribution with $n = 100$). Use this information to do each of the following:
 - a. Construct and interpret a 95% confidence interval to capture the true value of the proportion.
 - b. While playing, in one sample of 100 enemies, he found the item dropped 22 times. Does this provide evidence at the 0.01 level of significance that the actual drop rate is greater than 15.7%? Perform and interpret a complete hypothesis test.

2. A certain treatment is being tested for its effectiveness in suppressing flu symptoms. The researchers randomly assign treatments (placebo or new treatment) to individuals randomly selected from the population who have the flu and get the results that are detailed in the table below.

Group	Sample Size	Number with significant symptom alleviation
Placebo	576	201
New Treatment	576	239

- a. Does this provide significant evidence that the new treatment is better than a placebo? Perform a hypothesis test at the 0.05 level of significance.

- b. Construct a 95% confidence interval to capture the true difference between the treatment and the placebo. Does this result validate the results of the hypothesis test? Explain.

- The Recreation Department plans to collect data from a sample of 185 adult residents of the county and perform a test of significance at a significance level of 0.05 for the following hypotheses:

$$H_0 : p < 0.40$$

a. Describe a Type II error for this situation and describe a consequence of making this type of error.

- b. The Recreation Department recruits 185 adult residents who volunteer to take the physical fitness test. The test is passed by 85 out of the 185 residents, resulting in a z -score = 1.651 and a resulting p -value of 0.97 for the hypotheses stated above. If this was a reasonable test of significance for the hypotheses using the data collected from these 185 volunteers, what would the p -value of 0.97 lead you to conclude?
- c. Describe the primary flaw in the study described in part b.