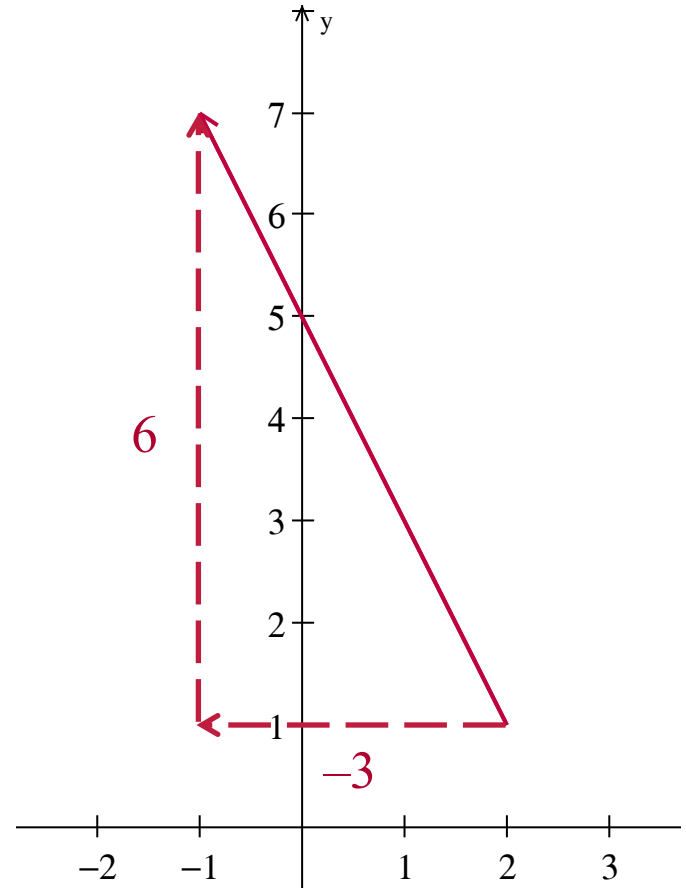


Find the component form, sketch and find the length of the vector with initial point (2, 1) and terminal point (−1, 7)

$$\langle -3, 6 \rangle$$

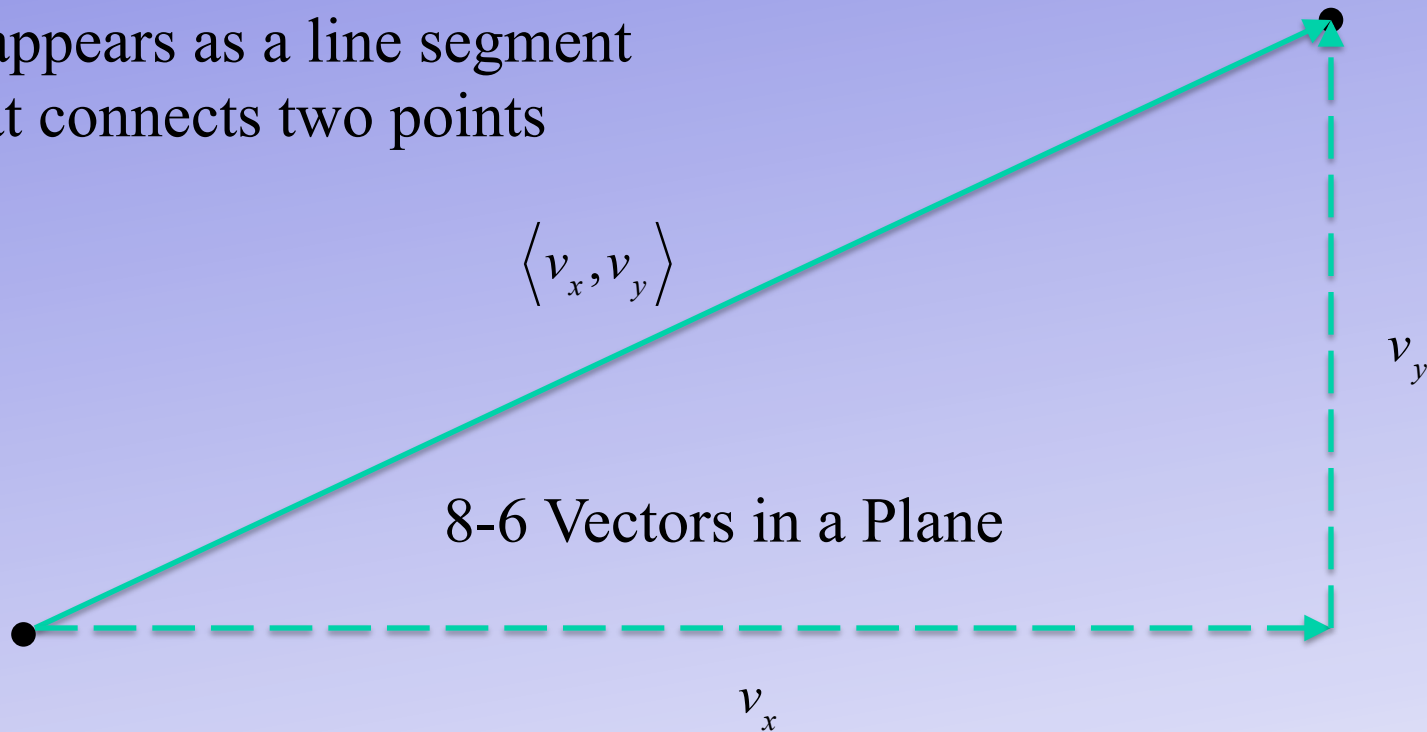
$$\sqrt{(-3)^2 + 6^2}$$

$$\sqrt{45} = 3\sqrt{5}$$



This is a Vector

It appears as a line segment
that connects two points

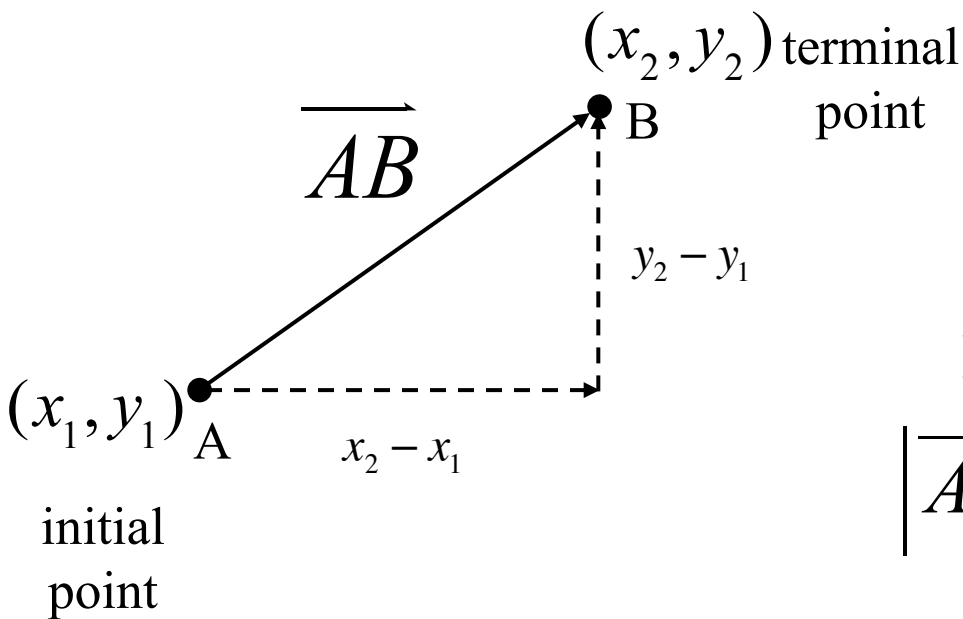


It also has something else: Direction

But the best part is it's really just the hypotenuse of a right triangle

What are those symbols next to each line segment?

We shall soon see.



The length of this vector is written as

$$|\overrightarrow{AB}|$$

It can be calculated like this:

$$|\overrightarrow{AB}| = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

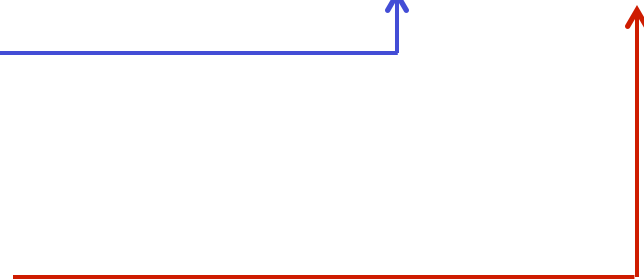
Look, it's just the distance formula

The component form of this vector is: $\overrightarrow{AB} = \langle x_2 - x_1, y_2 - y_1 \rangle$

*The horizontal
change in
position*



*The vertical
change in
position*



What is the component form of this vector?

$$\vec{w} = \langle 4 - 1, 5 - 1 \rangle$$

$$\vec{w} = \langle 3, 4 \rangle$$

What is the length (or magnitude) of this vector?

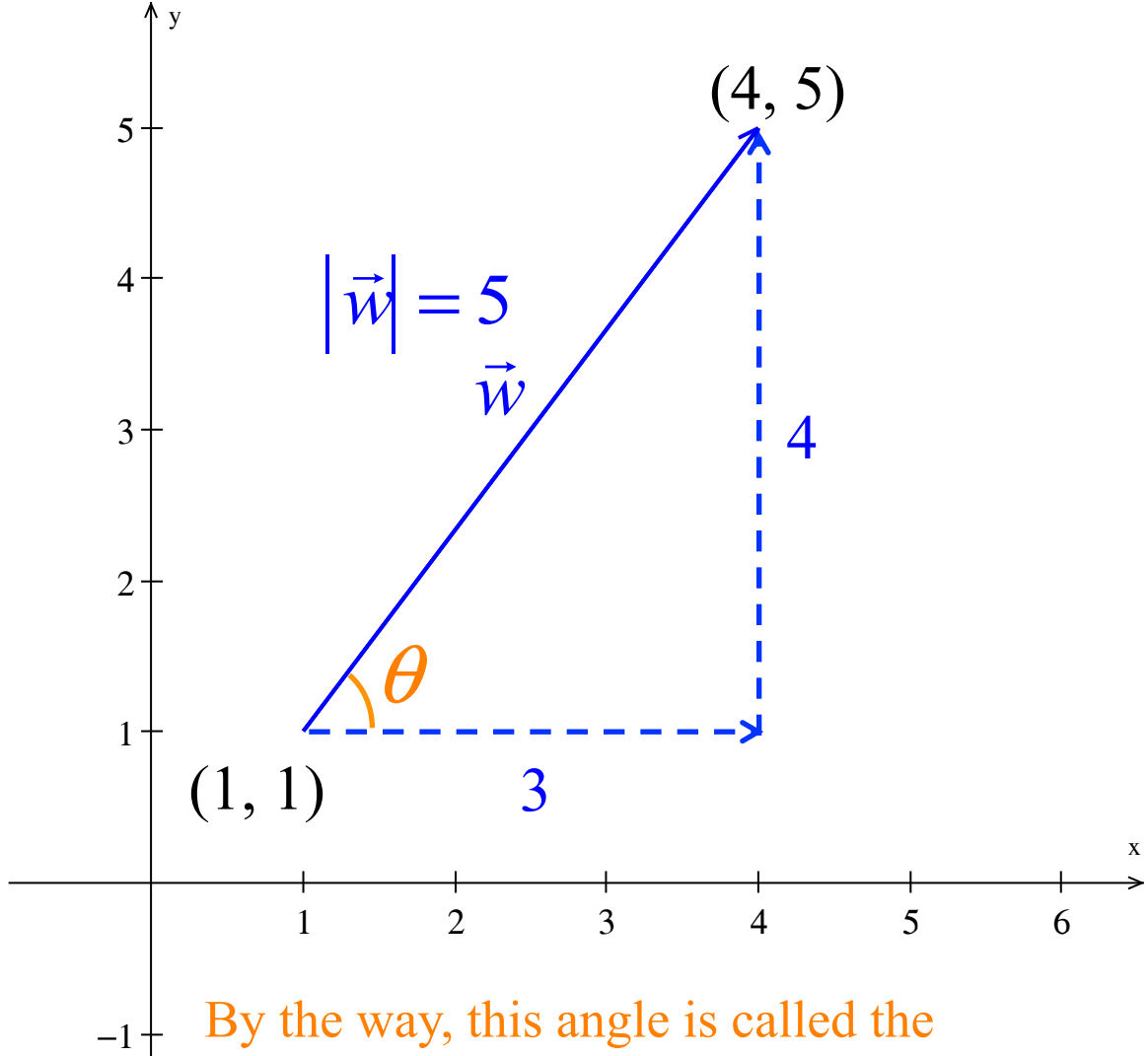
Remember that the vector is just the hypotenuse

$$|\vec{w}| = \sqrt{3^2 + 4^2} = 5$$

What is the measure of this angle?

Since $\tan \theta = \left(\frac{4}{3} \right)$ We'll just use the calculator

$$\theta = \tan^{-1} \left(\frac{4}{3} \right) \approx 53.13^\circ$$



By the way, this angle is called the direction that Greek symbol is called Theta

Let's add a vector

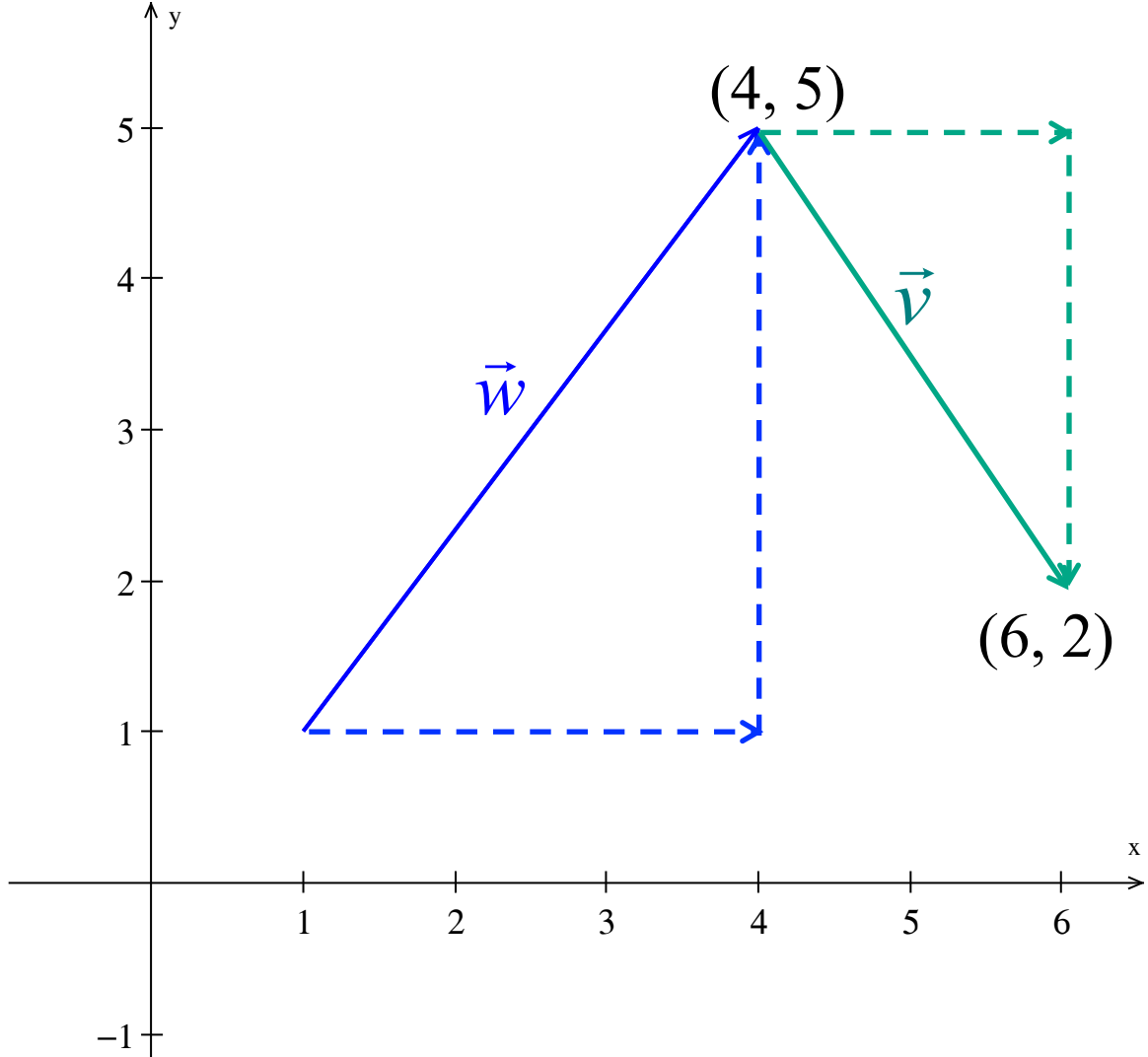
$$\vec{v} = \langle 6 - 4, 2 - 5 \rangle$$

$$\vec{v} = \langle 2, -3 \rangle$$

And the length of
this vector is

$$|\vec{v}| = \sqrt{2^2 + (-3)^2}$$

$$|\vec{v}| = \sqrt{4 + 9} = \sqrt{13}$$



Let's add these two vectors

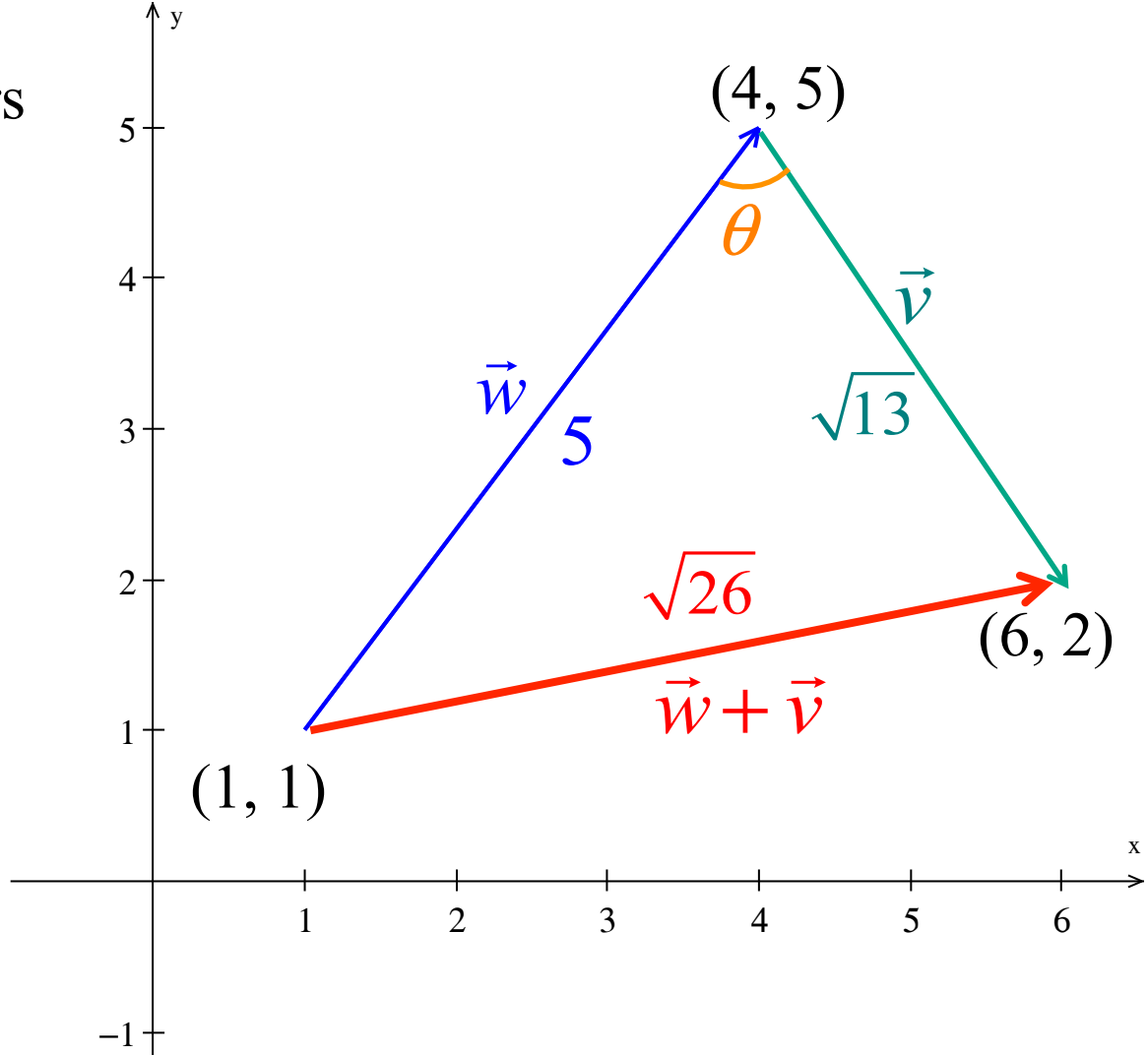
$$\vec{w} + \vec{v} = \langle 6 - 1, 2 - 1 \rangle$$

$$\vec{w} + \vec{v} = \langle 5, 1 \rangle$$

And the length of
this vector is

$$|\vec{w} + \vec{v}| = \sqrt{5^2 + 1^2}$$

$$|\vec{w} + \vec{v}| = \sqrt{26}$$



What is the measure of this angle?

Notice that we have an acute triangle and we know all three sides

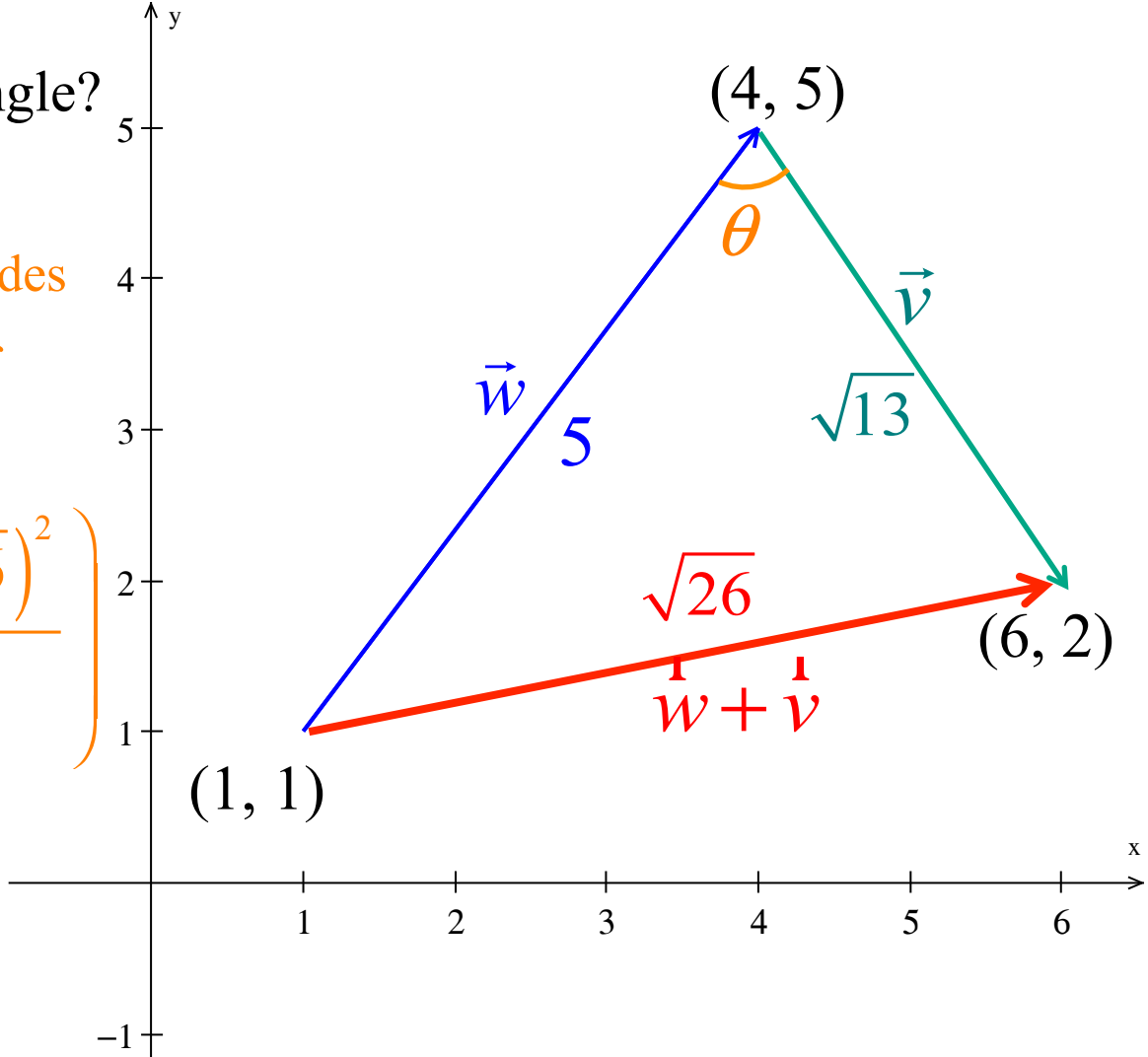
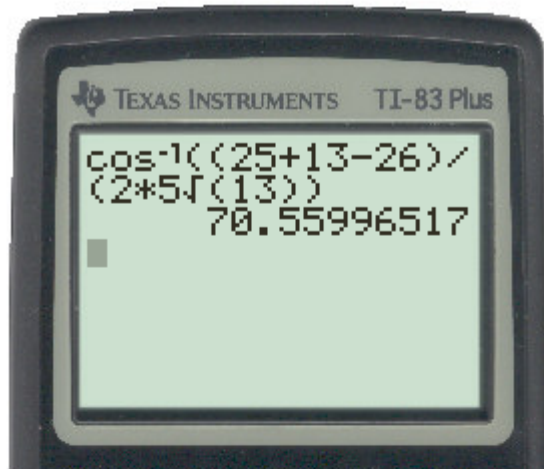
For this we will need the Law of Cosines

What is the measure of this angle?

Notice that we have an acute triangle and we know all three sides

For this we will need the Law of Cosines

$$\theta = \cos^{-1} \left(\frac{5^2 + (\sqrt{13})^2 - (\sqrt{26})^2}{2(5)\sqrt{13}} \right)$$



$$\theta \approx 70.56^\circ$$

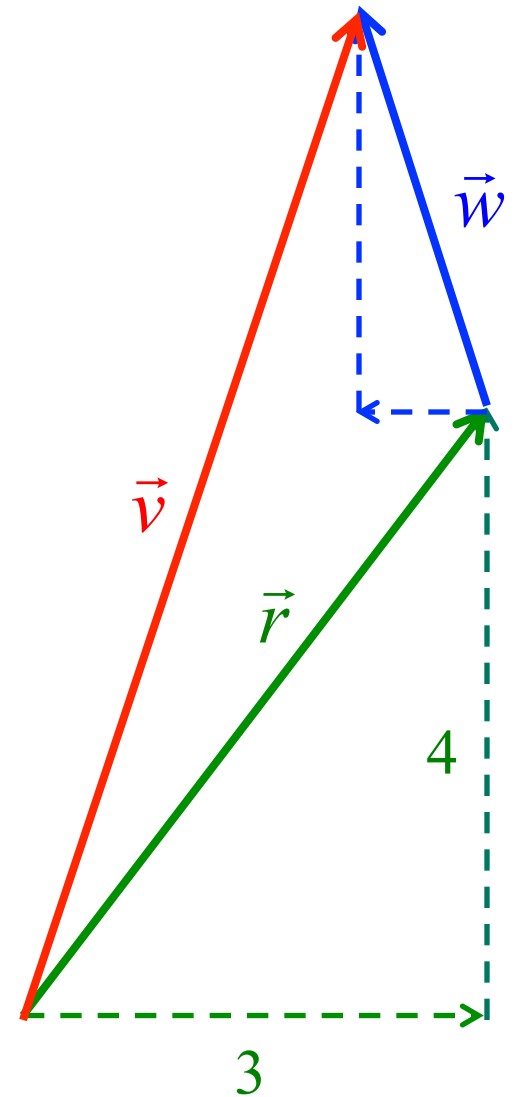
Now let's assume that this vector represents Mike May, Donovan Jones, and Mac Gates rowing a boat across Lake Merced at 5 mph.

The current of the lake is flowing in the direction of \vec{w}

$$\vec{r} = \langle 3, 4 \rangle \quad \vec{w} = \langle -1, 2 \rangle$$

How will the current affect the direction of their boat?

In other words find the resultant vector



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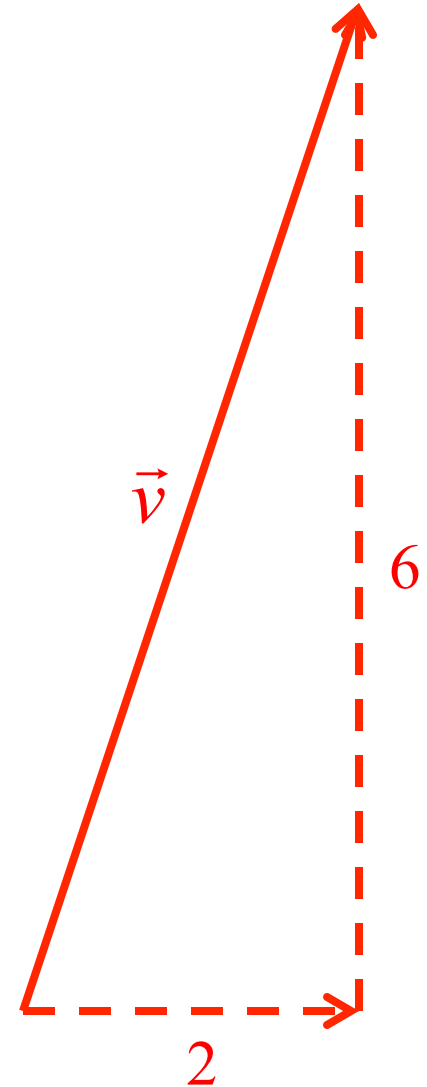
$$\vec{r} = \langle 3, 4 \rangle \quad \vec{w} = \langle -1, 2 \rangle$$

How will the current affect the direction of their boat?

In other words find the resultant vector

$$\begin{aligned} \vec{v} &= \vec{r} + \vec{w} = \langle 3, 4 \rangle + \langle -1, 2 \rangle = \\ &= \langle 2, 6 \rangle \end{aligned}$$

Assuming units of miles per hour, how fast are they going after the current affects them?



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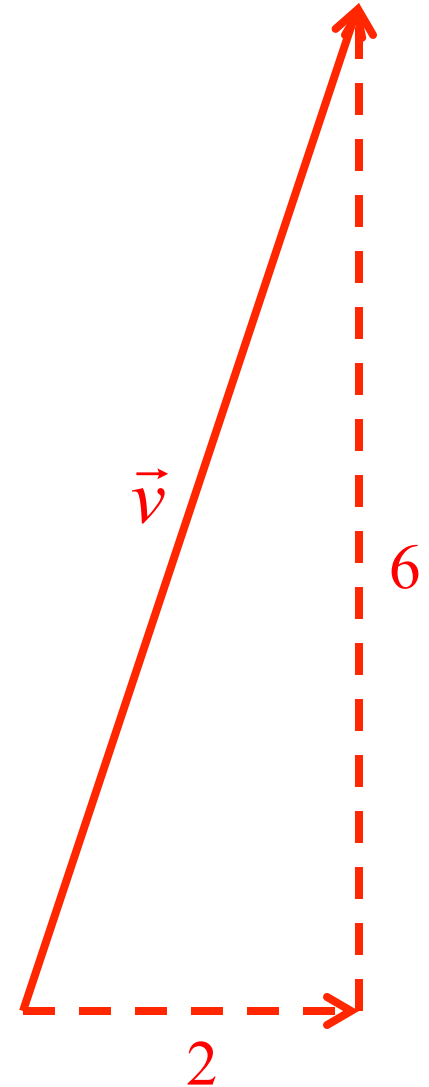
$$\vec{v} = \langle 2, 6 \rangle$$

Assuming units of miles per hour, how fast are they going after the current affects them?

In other words, what is the magnitude of the new vector?

$$|\vec{v}| = \sqrt{2^2 + 6^2}$$

$$|\vec{v}| = \sqrt{40} \approx 6.32 \text{ mph}$$



Now let's assume that this vector represents Mike May, Donovan Jones, and Mac Gates rowing a boat across Lake Merced at 5 mph.

The current of the lake is flowing in the direction of \vec{w}

How many degrees east of north are they now moving?

In other words what is the value of this angle?

$$\theta = \tan^{-1}\left(\frac{2}{6}\right) \approx 18.44^\circ$$

