Single Sample Hypothesis Tests for Means



Note #3: H_0 ALWAYS gets an = ...even if the wording in the problem sounds like it shouldn't

Note #2: Use only PARAMETERS in your hypothesis...although there will be some problems where we'll use words/sentences

Note #4: The symbol used in the alternate will come from the context of the problem

two-sided test, equivalent to a Confidence Interval (CI)
 - one-sided test

Steps in Hypothesis Testing

I. Define the population characteristic (i.e. parameter) about which hypotheses are to be tested.

- 2. State the null hypothesis H_0 .
- 3. State the alternative hypothesis H_a .
- 4. State the significance level for the test α .
- 5. Check all assumptions and state name of test.
- 6. State the name of the test.
- 7. State df if applicable (not applicable in proportion land).
- 8. Display the test statistic to be used without any computation at this point.
- 9. Compute the value of the test statistic, showing specific numbers used.
- 10. Calculate the P value.
- 11. Sketch a picture of the situation.
- 12. State the conclusion in two sentences -
 - I. Summarize in theory discussing H_0 .
 - 2. Summarize in context discussing H_a .

Single Sample Hypothesis Tests for Mean

Steps in Mean Hypothesis Testing

1. $\mu = \dots$ 2. $H_0 : \mu = \#$ \neq 3. $H_a : \mu < \#$ >

4. State the significance level for the test lpha .

8/9.
$$z = \frac{\overline{x} - \mu}{\sigma / \sqrt{n}} = \#$$

I. Random Sample

2. Normality stated $n \ge 30$

7. df = N/A

6. I Sample Mean *z* Test

Boxplot of raw data shows roughly symmetric shape

3. σ known



one-sided tests

two-sided tests



P(z > #) = normalcdf(#, 1E99, 0, 1) P(z < #) = normalcdf(-1E99, #, 0, 1) 2P(z > #) = 2 * normalcdf(#, 1E99, 0, 1) 2P(z < #) = 2 * normalcdf(-1E99, #, 0, 1)

12. State the conclusion in two sentences -1. Summarize in theory discussing H_0 . 2. Summarize in context discussing H_a .

Single Sample Hypothesis Tests for Mean

Steps in Mean Hypothesis Testing

1. $\mu = \dots$ 2. $H_0: \mu = \#$ \neq 3. $H_a: \mu < \#$

>

4. State the significance level for the test α .

8/9.
$$t = \frac{\overline{x} - \mu}{\sqrt[s]{\sqrt{n}}} = \#$$

 P_{-}

10.

$$P(t > \#) = tcdf(\#, 1E99, df)$$

$$P(t < \#) = tcdf(-1E99, \#, df)$$

$$2P(t > \#) = 2 * tcdf(\#, 1E99, df)$$

$$2P(t < \#) = 2 * tcdf(\#, 1E99, df)$$

12. State the conclusion in two sentences -1. Summarize in theory discussing H_0 . 2. Summarize in context discussing H_a .

- 5. Assumptions:
- I. Random Sample
- 2. Normality stated

 $n \ge 30$

6. I Sample Mean *t* Test

$$f = n - 1$$

Boxplot of raw data shows roughly symmetric shape

3. σ unknown



one-sided tests

two-sided tests



$$P(t > \#) = tcdf(\#, 1E99, df)$$

$$P - value = P(t < \#) = tcdf(-1E99, \#, df)$$

$$2P(t > \#) = 2 * tcdf(\#, 1E99, df)$$

$$2P(t < \#) = 2 * tcdf(-1E99, \#, df)$$

10.

one-sided tests

two-sided tests

Finding P-Values for a t Test 1. Upper-tailed test: t curve for n - 1 df $H_a: \mu >$ hypothesized value. P-value = area in upper tail P-value computed as illustrated: 0 Calculated t 2. Lower-tailed test: t curve for n - 1 df $H_a: \mu <$ hypothesized value. P-value = area in lower tail *P*-value computed as illustrated: 0 Calculated t *P*-value = sum of area in two tails t curve for n - 1 df

3. Two-tailed test: $H_a: \mu \neq$ hypothesized value. P-value computed as illustrated:



0

P-Value < $\alpha \Rightarrow$ **Reject** H_o , **Evidence for** H_a

P-Value > $\alpha \Rightarrow$ Fail to Reject H_o , No Evidence for H_a



P-Value is the probability of obtaining a test statistic at least as extreme as the one that was actually observed, assuming that the null hypothesis is true



Errors - We make them, even though we're awesome



Type I error - reject H_0 when H_0 is true Type II error - fail to reject H_0 when H_0 is false OR

Type I error - Ist equation correct and you pick the 2nd equation Type II error - 2nd equation correct and you pick the 1st equation

α vs β

 $P(\text{Type I error}) = \alpha \leftarrow$ $P(\text{Type II error}) = \beta$

Also called 'level of significance' or 'significance level'.

If α goes up, then β goes down. If α goes down, then β goes up.

Game plan - determine which error is worse, then choose the appropriate α and β .

Some common terminology -

"Justify" = Run a hypothesis test "Estimate" = Construct a Confidence Interval "Statistically significant" = The null hypothesis is rejected